

**ADDENDUM #2 TO P11.**

**The Sigma Particles, ( $J = 1/2\hbar$ ).**

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## **Abstract.**

This Addendum provides details of the energy distribution of the quarks that make up all Sigma sub-atomic particles. Also presented are the energy translations that take place during their decay. This is augmented by further discussion of the decay process itself.

This is the second Addendum to P11, "Derivation of the Quark Energy Distributions and Decay Products of Baryonic Sub-Atomic Particles".

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## References

## **1.0 Introduction.**

There are nine Sigma particles with  $J = 1/2\hbar$ , as shown in the following brief table, with their quark complement.

<b>Particle</b>	<b>Quarks</b>
$\Sigma^+$	uus
$\Sigma^0$	uds
$\Sigma^-$	dds
$\Sigma_c^+$	udc
$\Sigma_c^0$	ddc
$\Sigma_c^{++}$	uuc
$\Sigma_b^+$	uub
$\Sigma_b^-$	ddb
$\Sigma_b^0$	udb

**Table 1.1 - The Sigma Particles.**

It will be shown that  $\Sigma^0$ ,  $\Sigma_c^+$  and  $\Sigma_b^0$  are high confinement energy versions of  $\Lambda^0$ ,  $\Lambda_c^+$  and  $\Lambda_b^0$  respectively, as they contain the same quark complement. As a consequence, the decay of the former to the latter, takes place without a quark flavour change and is a confinement energy only decay.

Unlike the Lambda particles, the Sigma particles only exhibit a total of 12 decay paths and of these it is only  $\Sigma^+$  and  $\Sigma^-$  that exhibit more than one. However, the 12 decay paths involve a total of eight decay types of which seven are different from those exhibited by the Lambda particles. It is for these seven that full details are provided in this Addendum. The details to be shown are as follows.

- (i) The Intrinsic Angular Momentum Configurations, (from the generalised tables provided in [3]).
- (ii) The Quark Energy Distributions, (These are calculated from the basic theory in [3]).
- (iii) The Decay Energy Translations, (These are calculated using the decay process described in [3], as augmented in [4] and, as necessary, by Section 3.1 in this Addendum).

Note that as in [3] and [4], only particles with  $J = 1/2\hbar$  containing quarks with  $J = \pm 1/2\hbar$  are considered in this Addendum.

Also note that energy will be represented as equivalent mass via the units  $\text{MeV}/c^2$ , which for conciseness will be assumed and therefore omitted in the text.

Finally, for a full appreciation of this paper, it is recommended that [3] and [4] be read first.

## **2.0 Nomenclature.**

In this Addendum, the following nomenclature will be used.

- P Indicates any Baryon.
- P(#) Indicates the type of intrinsic angular momentum configuration of P.
- q# Indicates the #th quark in P.
- $E_c$  Indicates quark confinement energy.
- $E_k$  Indicates kinetic energy.
- Indicates a particle decay.
- ⇒ Indicates a quark flavour change.

### **3.0 Initial Discussions.**

#### **3.1 The Interim Energy Distribution - A Further variation.**

In [3] it was shown that the decay process of the example shown there only involved a single quark flavour change to one at a lower level, (down) i.e.  $d \Rightarrow u$ . In [4] decays of the Lambda particles involved three types of quark flavour change, (i) a single change down, (ii) a double change down, and (iii) a double change, one down and one up, i.e.  $u \Rightarrow d$ . In all of these the major quark to change flavour was the one possessing the greatest total energy. In this Addendum two further types appear, (i) a single change down, and (ii) a single change up, where in both cases the quark that changes flavour is not the highest total energy quark. The mechanism that triggers these events is discussed in Section 5.0.

#### **3.2 Decay Distribution Patterns - Overall Summary.**

This summary lists the primary decay products of the nine Sigma particles according to their intrinsic angular momentum configurations. Included are the branching fractions from [2], which have been augmented via inclusion of their minor decay products, to raise the overall branching fraction to 100% for each Sigma. Also included is indication of the seven decays for which full details are provided in Section 4.0.

<b>P(1)</b>	<b>P(2)</b>	<b>P(3)</b>	<b>Branching Fraction, (%)</b>	<b>Full Details Provided</b>
$\Sigma^+(1)$	$\Sigma^+(2)$			
$p^+(1)$	$p^+(2)$		51.57	
$n^0(1)$	$n^0(2)$		48.31	√
$\Lambda^0(2)$	$\Lambda^0(3)$		0.12	√
$\Sigma^0(1)$	$\Sigma^0(2)$	$\Sigma^0(3)$		
$\Lambda^0(1)$	$\Lambda^0(2)$	$\Lambda^0(3)$	100	√
$\Sigma^-(1)$	$\Sigma^-(2)$			
$n^0(1)$	$n^0(2)$		99.85	
$\Lambda^0(2)$	$\Lambda^0(3)$		0.15	√
$\Sigma_c^+(1)$	$\Sigma_c^+(2)$	$\Sigma_c^+(3)$		
$\Lambda_c^+(1)$	$\Lambda_c^+(2)$	$\Lambda_c^+(3)$	100	
$\Sigma_c^0(1)$	$\Sigma_c^0(2)$			
$\Lambda_c^+(2)$	$\Lambda_c^+(3)$		100	
$\Sigma_c^{++}(1)$	$\Sigma_c^{++}(2)$			
$\Lambda_c^+(2)$	$\Lambda_c^+(3)$		100	√

$\Sigma_b^+(1)$	$\Sigma_b^+(2)$			
$\Lambda_b^0(2)$	$\Lambda_b^0(3)$		100	$\checkmark$
$\Sigma_b^-(1)$	$\Sigma_b^-(2)$			
$\Lambda_b^0(2)$	$\Lambda_b^0(3)$		100	$\checkmark$
$\Sigma_b^0(1)$	$\Sigma_b^0(2)$	$\Sigma_b^0(3)$		
$\Lambda_b^0(1)$	$\Lambda_b^0(2)$	$\Lambda_b^0(3)$	100	

**Table 3.1 - Overall Summary of Decay Configuration Patterns.**

Note: In Table 3.1 the decay of  $\Sigma_b^0$  is reported in [2] and [3] as unknown. This is discussed in Section 4.9.

### 3.3 Type of Decay.

The types of decay exhibited by all Sigma particles is shown in the table below. These types arise according to, in The Interim Energy Distribution Tables, the nature of the quark flavour change(s), and how the quark confinement energy varies.

Decay Type	Particle Decay	Interim Energy Distribution - Confinement Energy Sign			Quark Flavour Change	
		$q_1$	$q_2$	$q_3$	Down	Up
1	$\Sigma^+ \rightarrow p^+$	+ve	+ve	+ve	$q_3$	
11	$\rightarrow n^0$	-ve	+ve	+ve	$q_3$	$q_2$
7	$\rightarrow \Lambda^0$	+ve	+ve	+ve		$q_2$
8	$\Sigma^0 \rightarrow \Lambda^0$	+ve	+ve	+ve		
8	$\Sigma_c^+ \rightarrow \Lambda_c^+$	+ve	+ve	+ve		
1	$\Sigma^- \rightarrow n^0$	+ve	+ve	+ve	$q_3$	
1 $\phi$	$\rightarrow \Lambda^0$	+ve	+ve	+ve	$q_2$	
1 $\phi$	$\Sigma_c^0 \rightarrow \Lambda_c^+$	+ve	+ve	+ve	$q_2$	
9	$\Sigma_c^{++} \rightarrow \Lambda_c^+$	-ve	+ve	+ve		$q_2$
10	$\Sigma_b^+ \rightarrow \Lambda_b^0$	-ve	-ve	+ve		$q_2$
2 $\phi$	$\Sigma_b^- \rightarrow \Lambda_b^0$	-ve	-ve	+ve	$q_2$	
8*	$\Sigma_b^0 \rightarrow \Lambda_b^0$	+ve	+ve	+ve		

**Table 3.2 - Types of Decay Exhibited by Sigma Particles.**

Note that Decay Type 8 is a confinement energy only decay, there is no quark flavour change.

1 $\phi$  This decay is classified as Type 1 but with  $q_2$  changing flavour instead of  $q_3$ , ( $q_2$  has less total energy than  $q_3$ ).

- 2φ This decay is classified as Type 2 but with  $q_2$  changing flavour instead of  $q_3$ .
- \* This decay is reported as unknown in [2] and [3] but because  $\Sigma_b^0$  and  $\Lambda_b^0$  have the same quark complement, (udb), it is expected that  $\Sigma_b^0$  will decay to  $\Lambda_b^0$  via Decay Type 8.

#### **4.0 Intrinsic Angular Momentum Configuration Tables, Energy Distribution Tables and Decay Energy Translations.**

##### **4.1 The $\Sigma^+$ Particle.**

###### **4.1.1. Intrinsic Angular Momentum Configuration.**

The  $\Sigma^+$  particle contains two identical quarks and can therefore exist in only two configurations.

$\Sigma^+(\#)$	$u_1$	$u_2$	$s_1$	Decay Modes
1	↑	↓	↑	$\Sigma^+(s_1) \Rightarrow n^0(d_1)$ and $\Sigma^+(u_2) \Rightarrow n^0(d_2)$
2	↓	↑	↑	$\Sigma^+(s_1) \Rightarrow n^0(d_2)$ and $\Sigma^+(u_1) \Rightarrow n^0(d_1)$

**Table 4.1 - Intrinsic Angular Momentum Configuration of  $\Sigma^+$ .**

In Table 4.1 each arrow represents the direction of an intrinsic angular momentum of  $J = 1/2\hbar$ .

###### **4.1.2. Energy Distribution Table.**

This is determined from the basic theory in [3], is shown in the following table, and is applicable to both configurations in Table 4.1 above.

Energy	$u_1$	$u_2$	$s_1$	Total
Matter	2.40	2.40	100.00	104.80
Resonance	47.79	47.79	1.15	96.73
Confinement	22.62	22.62	942.61	987.85
Total	72.81	72.81	1043.76	1189.38

**Table 4.2 - Energy Distribution for  $\Sigma^+$ .**

###### **4.1.3. Decay Energy Translations.**

(i) Decay  $\Sigma^+ \rightarrow n^0$ , (Decay type 11).

The decay process here is identical to that described in [4], Section 3.1, (for decay Type 4), and is similar to Type 4 with the exception that in the Interim Energy Distribution Table the sign of the confinement energy for  $q_2$  is positive instead of negative.

Energy	$u_1$	$\Sigma^+(u_2) \Rightarrow n^0(d_2)$	$\Sigma^+(s_1) \Rightarrow n^0(d_1)$	Total
Matter	2.40	4.75	4.75	11.90
Resonance	72.73	36.75	36.75	146.23
Confinement	-2.32	31.31	1002.26	1031.25
Total	72.81	72.81	1043.76	1189.38

**Table 4.3 - Interim Energy Distribution for  $\Sigma^+ \rightarrow n^0$ .**

The decay is completed by the following confinement energy translations.

- $E_c(u_1)$  Increases via absorption from  $d_1$  by 159.92 to 157.60, (the Neutron level).
- $E_c(d_2)$  Increases via absorption from  $d_1$  by 280.61 to 311.92, (the Neutron level).
- $E_c(d_1)$  Therefore decreases by 440.53 to 561.73.

Finally,  $d_1$  ejects 249.81 in the form of a  $\pi^+$  Pion plus  $E_k$  to reduce to 311.92, the Neutron level. This completes the decay.

(i) Decay  $\Sigma^+ \rightarrow \Lambda^0$ , (Decay Type 7).

This decay is considered unusual in that it is not the quark with the highest total energy that changes flavour. The process is discussed in Section 5.0. The Interim Energy Distribution Table is as follows

Energy	$u_1$	$\Sigma^+(u_2) \Rightarrow \Lambda^0(d_1)$	$s_1$	Total
Matter	2.40	4.75	100.00	107.15
Resonance	62.47	31.56	1.50	95.53
Confinement	7.94	36.50	942.26	986.70
Total	72.81	72.81	1043.76	1189.38

**Table 4.4 - Interim Energy Distribution for  $\Sigma^+ \rightarrow \Lambda^0$ .**

The quark confinement energy translations are then

- $E_c(u_1)$  Increases via absorption from  $s_1$  by 12.51 to 20.45, (the  $\Lambda^0$  level).
- $E_c(d_1)$  Increases via absorption from  $s_1$  by 3.97 to 40.47, (the  $\Lambda^0$  level).
- $E_c(s_1)$  Therefore decreases by 16.48 to 925.78.

Finally,  $s_1$  ejects 73.70 as an  $e^+ + \nu_e + E_k$  and reduces to 852.08, the  $\Lambda^0$  level.

**4.2 The  $\Sigma^0$  Particle.**

**4.2.1. Intrinsic Angular Momentum Configuration.**

This particle has the same quark complement as  $\Lambda^0$  and therefore has the same Intrinsic Angular Momentum Configuration.

$\Sigma^0(\#)$	$u_1$	$d_1$	$s_1$	Decay Mode
1	↑	↑	↓	$\Sigma^0 \rightarrow \Lambda^0$
2	↑	↓	↑	
3	↓	↑	↑	

**Table 4.5 - Intrinsic Angular Momentum Configuration of  $\Sigma^0$ .**

4.2.2. Energy Distribution table and Decay Energy Translations.

Energy	u <sub>1</sub>	d <sub>1</sub>	s <sub>1</sub>	Total
Matter	2.4	4.75	100.00	107.15
Resonance	62.47	31.56	1.50	95.53
Confinement	22.17	43.89	923.90	989.96
Total	87.04	80.20	1025.40	1192.64

**Table 4.6 - Energy Distribution for  $\Sigma^0$ .**

Table 4.6 also represents the Interim Energy Distribution for the decay of  $\Sigma^0$  to  $\Lambda^0$  because with identical quark complements the matter and resonance energies are the same. The decay is therefore via confinement energy translation only, Decay Type 8. The confinement energy translations are as follows

- $E_c(u_1)$  Decreases by 1.72 to 20.45, (the  $\Lambda^0$  level).
- $E_c(d_1)$  Decreases by 3.42 to 40.47, (the  $\Lambda^0$  level).
- $E_c(s_1)$  Decreases by 71.82 to 852.08, (the  $\Lambda^0$  level).

The sum of the above reductions, 76.96, is then ejected as Gamma radiation.

**4.3 The  $\Sigma^-$  Particle.**

**4.3.1. Intrinsic Angular Momentum Configuration.**

This is similar to that for  $\Sigma^+$

$\Sigma^-$ (#)	d <sub>1</sub>	d <sub>2</sub>	s <sub>1</sub>	Decay Modes
1	↑	↓	↑	$\Sigma^-(s_1) \Rightarrow n^0(u_1)$ or $\Sigma^-(d_1) \Rightarrow \Lambda^0(u_1)$
2	↓	↑	↑	$\Sigma^-(s_1) \Rightarrow n^0(u_1)$ or $\Sigma^-(d_2) \Rightarrow \Lambda^0(u_1)$

**Table 4.7 - Intrinsic Angular Momentum of  $\Sigma^-$ .**

**4.3.2. Energy Distribution.**

Energy	d <sub>1</sub>	d <sub>2</sub>	s <sub>1</sub>	Total
Matter	4.75	4.75	100.00	109.50
Resonance	46.34	46.34	2.20	94.88
Confinement	43.08	43.08	906.92	993.08
Total	94.17	94.17	1009.12	1197.46

**Table 4.8 - Energy Distribution for  $\Sigma^-$ .**

**4.3.3. Decay Energy Translations.**

**(i) Decay  $\Sigma^- \rightarrow \Lambda^0$ , (Decay Type 1 $\phi$ ).**

The Interim Energy Distribution for this decay is as follows.

Energy	d <sub>1</sub>	Σ <sup>-</sup> (d <sub>2</sub> )→Λ <sup>0</sup> (u <sub>1</sub> )	s <sub>1</sub>	Total
Matter	4.75	2.40	100.00	107.15
Resonance	31.56	62.47	1.50	95.53
Confinement	57.86	29.30	907.62	985.78
Total	94.17	94.17	1009.12	1197.46

**Table 4.9 - Interim Energy Distribution for Σ<sup>-</sup>→Λ<sup>0</sup>.**

This decay only occurs with a branching fraction of 0.15%. For the other 99.85% it is s<sub>1</sub> that changes flavour to a u quark to realise Σ<sup>-</sup>→n<sup>0</sup> as a Type 1 decay. The process for this variation, Σ<sup>-</sup>→Λ<sup>0</sup>, is discussed in Section 5.0.

The confinement energy translations are as follows.

$E_c(d_1)$  Decreases by 17.39 to 40.47, (the Λ<sup>0</sup> level).

$E_c(s_1)$  Decreases by 55.74 to 852.08, (the Λ<sup>0</sup> level).

$E_c(u_1)$  Therefore increases by 72.93 to 102.23.

Finally, u<sub>1</sub> ejects 81.75 as an e<sup>-</sup> + ν<sub>e</sub> + E<sub>k</sub> and reduces to 20.45, the Λ<sup>0</sup> level. This completes the decay.

#### **4.4 The Σ<sub>c</sub><sup>+</sup> Particle.**

##### **4.4.1. Intrinsic Angular Momentum Configuration.**

This particle has the same quark complement as Λ<sub>c</sub><sup>+</sup> and therefore has the same Intrinsic Angular Momentum Configuration.

Σ <sub>c</sub> <sup>+</sup> (#)	u <sub>1</sub>	d <sub>1</sub>	c <sub>1</sub>	Decay Mode
1	↑	↑	↓	Σ <sub>c</sub> <sup>+</sup> → Λ <sub>c</sub> <sup>+</sup>
2	↑	↓	↑	
3	↓	↑	↑	

**Table 4.10 - Intrinsic Angular Momentum Configuration for Σ<sub>c</sub><sup>+</sup>.**

##### **4.4.2. Energy Distribution.**

Energy	u <sub>1</sub>	d <sub>1</sub>	c <sub>1</sub>	Total
Matter	2.40	4.75	1250	1257.15
Resonance	21.43	10.83	0.04	32.30
Confinement	2.22	4.40	1156.83	1163.45
Total	26.05	19.98	2406.87	2452.90

**Table 4.11 - Energy Distribution of Σ<sub>c</sub><sup>+</sup>.**

4.4.3. Decay Energy Translations.

This particle decays to  $\Lambda_c^+$  via Decay Type 8, a confinement energy only decay due to possessing the same quark complement.

**4.5 The  $\Sigma_c^0$  Particle.**

4.5.1. Intrinsic Angular Momentum Configuration.

This is similar to that for  $\Sigma^-$ .

$\Sigma_c^0$ (#)	$d_1$	$d_2$	$c_1$	Decay Modes
1	↑	↓	↑	$\Sigma_c^0(d_1) \Rightarrow \Lambda_c^+(u_1)$
2	↓	↑	↑	$\Sigma_c^0(d_1) \Rightarrow \Lambda_c^+(u_1)$

**Table 4.12 - Intrinsic Angular Momentum Configuration for  $\Sigma_c^0$ .**

4.5.2. Energy Distribution.

Energy	$d_1$	$d_2$	$c_1$	Total
Matter	4.75	4.75	1250	1259.50
Resonance	16.23	16.23	0.06	32.52
Confinement	4.38	4.38	1152.95	1161.71
Total	25.36	25.36	2403.01	2453.73

**Table 4.13 - Energy Distribution of  $\Sigma_c^0$ .**

4.5.3. Decay Energy Translations.

This particle decays to  $\Lambda_c^+$  via Decay Type 1 $\phi$ .

**4.6 The  $\Sigma_c^{++}$  Particle.**

4.6.1. Intrinsic Angular Momentum Configuration.

This is similar to those for  $\Sigma_c^0$  and  $\Sigma^-$ .

$\Sigma_c^{++}$ (#)	$u_1$	$u_2$	$c_1$	Decay Modes
1	↑	↓	↑	$\Sigma_c^{++}(u_2) \Rightarrow \Lambda_c^+(d_1)$
2	↓	↑	↑	$\Sigma_c^{++}(u_2) \Rightarrow \Lambda_c^+(d_1)$

**Table 4.13 - Intrinsic Angular Momentum Configuration for  $\Sigma_c^{++}$ .**

**4.6.2. Energy Distribution.**

Energy	u <sub>1</sub>	u <sub>2</sub>	c <sub>1</sub>	Total
Matter	2.40	2.40	1250	1254.80
Resonance	15.99	15.99	0.03	32.01
Confinement	2.23	2.23	1162.71	1167.17
Total	20.62	20.62	2412.74	2453.98

**Table 4.15 - Energy Distribution of  $\Sigma_c^{++}$ .**

**4.6.3. Decay Energy Translations.**

This particle decays to  $\Lambda_c^+$  via Decay Type 9 in which the only difference to Type 7 is that in the Interim Energy Distribution Table the sign of the confinement energy of q<sub>1</sub> is negative instead of positive.

Energy	u <sub>1</sub>	$\Sigma_c^{++}(u_2) \Rightarrow \Lambda_c^+(d_1)$	c <sub>1</sub>	Total
Matter	2.40	4.75	1250	1257.15
Resonance	21.43	10.83	0.04	32.30
Confinement	-3.21	5.04	1162.70	1164.53
Total	20.62	20.62	2412.74	2453.98

**Table 4.16 - Interim Energy Distribution for  $\Sigma_c^{++} \rightarrow \Lambda_c^+$ .**

The quark confinement energy translations are then

$E_c(u_1)$  Increases via absorption from c<sub>1</sub> by 5.11 to 1.9, (the  $\Lambda_c^+$  level).

$E_c(c_1)$  Decreases by 171.36 to 991.34, (the  $\Lambda_c^+$  level).

$E_c(d_1)$  Therefore increases by 166.25 to 171.29.

Finally, d<sub>1</sub> ejects 167.52 as a  $\pi^+$  Pion +  $E_k$  and reduces to 3.77 the  $\Lambda_c^+$  level.

**4.7 The  $\Sigma_b^+$  Particle.**

**4.7.1. Intrinsic Angular Momentum Configuration.**

This is similar to those for  $\Sigma_c^0$  etc.

$\Sigma_b^+$ (#)	u <sub>1</sub>	u <sub>2</sub>	b <sub>1</sub>	Decay Modes
1	↑	↓	↑	$\Sigma_b^+(u_2) \Rightarrow \Lambda_c^+(d_1)$
2	↓	↑	↑	$\Sigma_b^+(u_2) \Rightarrow \Lambda_c^+(d_1)$

**Table 4.17 - Intrinsic Angular Momentum Configuration for  $\Sigma_b^+$ .**

### 4.7.2. Energy Distribution.

Energy	$u_1$	$u_2$	$b_1$	Total
Matter	2.40	2.40	4300	4304.80
Resonance	5.20	5.20	0.003	10.40
Confinement	0.83	0.83	1494.43	1496.09
Total	8.43	8.43	5794.43	5811.29

**Table 4.18 - Energy Distribution for  $\Sigma_b^+$**

### 4.7.3. Decay Energy Translations.

This particle decays to  $\Lambda_b^0$  via Decay Type 10 in which the only difference to Type 9 is that in the Interim Energy Distribution Table the sign of the confinement energy of  $q_2$  is negative instead of positive.

Energy	$u_1$	$\Sigma_b^+(u_2) \Rightarrow \Lambda_b^0(d_1)$	$b_1$	Total
Matter	2.4	4.75	4300	4307.15
Resonance	58.74	29.68	0.033	88.45
Confinement	-52.71	-26.00	1494.40	1415.69
Total	8.43	8.43	5794.43	5811.29

**Table 4.19 - Interim Energy Distribution for  $\Sigma_b^+ \rightarrow \Lambda_b^0$ .**

The confinement energy translations are as follows

$E_c(u_1)$  Increases via absorption from  $b_1$  by 53.39 to 0.68, (the  $\Lambda_b^0$  level).

$E_c(b_1)$  Decreases by 272.63 to 1221.77, (the  $\Lambda_b^0$  level).

$E_c(d_1)$  Therefore increases by 219.24 to 193.24.

Finally  $d_1$  ejects 191.89 as a  $\pi^+$  pion +  $E_k$  and reduces to 1.35, the  $\Lambda_b^0$  level. This completes the decay.

In the Interim Energy Distribution Table the quark confinement energy of  $u_1$  and  $\Sigma_b^+(u_2) \Rightarrow \Lambda_b^0(d_1)$  are both negative indicating the confinement force between them has become repulsive. However, the particle at this stage is still held together by the excessive confinement force possessed by  $b_1$ . This is similar to the decay of  $\Lambda_c^+$  to  $\Lambda^0$  in [4], (see [4] Appendix A for supporting analysis).

## **4.8 The $\Sigma_b^-$ Particle.**

### 4.8.1. Intrinsic Angular Momentum Configuration.

This is similar to most other Sigma particles.

$\Sigma_b^-$ (#)	$d_2$	$d_1$	$b_1$	Decay Modes
1	↑	↓	↑	$\Sigma_b^- (d_1) \Rightarrow \Lambda_b^0 (u_1)$
2	↓	↑	↑	$\Sigma_b^- (d_1) \Rightarrow \Lambda_b^0 (u_1)$

**Table 4.20 - Intrinsic Angular Momentum Configuration for  $\Sigma_b^-$ .**

**4.8.2. Energy Distribution.**

Energy	$d_2$	$d_1$	$b_1$	Total
Matter	4.75	4.75	4300	4309.50
Resonance	4.89	4.89	0.005	9.79
Confinement	1.65	1.65	1492.90	1496.20
Total	11.29	11.29	5792.91	5815.49

**Table 4.21 - Energy Distribution for  $\Sigma_b^-$ .**

**4.8.3. Decay Energy Translations.**

This particle decays to  $\Lambda_b^0$  via Decay Type  $2\phi$  which is similar to Type  $1\phi$  except that in the Interim Energy Distribution Table the confinement energy of both  $q_1$  and  $q_2$  is negative instead of positive. This table is as follows

Energy	$d_2$	$\Sigma_b^- (d_1) \Rightarrow \Lambda_b^0 (u_1)$	$b_1$	Total
Matter	4.75	2.40	4300	4307.15
Resonance	29.68	58.74	0.033	88.45
Confinement	-23.13	-49.84	1492.88	1419.91
Total	11.30	11.30	5792.91	5815.51

**Table 4.22 - Interim Energy Distribution for  $\Sigma_b^- \rightarrow \Lambda_b^0$ .**

The comments above with regard to the negative quark confinement energies of  $\Sigma_b^- (d_1) \Rightarrow \Lambda_b^0 (u_1)$  and  $d_2$  equally apply here. The final confinement energy translations are as follows.

$E_c(u_1)$  Increases via absorption from  $b_1$  by 50.52 to 0.68, (the  $\Lambda_b^0$  level).

$E_c(d_2)$  Increases via absorption from  $b_1$  by 24.48 to 1.35, (the  $\Lambda_b^0$  level).

$E_c(b_1)$  Therefore decreases by 75.00 to 1414.88.

Finally,  $b_1$  ejects 196.11 in the form of a  $\pi^-$  pion +  $E_k$  and reduces to 1221.77, the  $\Lambda_b^0$  level. This completes the decay.

## 4.9 The $\Sigma_b^0$ Particle.

### 4.9.1. Intrinsic Angular Momentum Configuration.

This is identical to  $\Lambda_b^0$ .

$\Sigma_b^0$ (#)	$u_1$	$d_1$	$b_1$	Decay Modes
1	↑	↑	↓	$\Sigma_b^0 \rightarrow \Lambda_b^0$
2	↑	↓	↑	
3	↓	↑	↑	

**Table 4.23 - Intrinsic Angular Momentum Configuration for  $\Sigma_b^0$ .**

### 4.9.2. Energy Distribution.

Energy	$u_1$	$d_1$	$b_1$	Total
Matter	2.40	4.75	4300	4307.15
Resonance	58.74	29.68	0.033	88.45
Confinement	0.74	1.47	1334.00	1337.21
Total	61.88	35.90	5634.03	5732.81

**Table 4.24 - Energy Distribution for  $\Sigma_b^0$ .**

### 4.9.3. Decay Energy Translations.

The decay of this particle is reported as unknown in [1] and [2]. However, it has the same quark complement as  $\Lambda_b^0$  and will therefore exhibit the same matter and resonance energies. It will therefore decay to  $\Lambda_b^0$  via Decay Type 8 as per similar Sigma particles reviewed here.

## 5.0 Conclusions.

There are four aspects of this Addendum worthy of discussion. The first is that there are seven extra Decay Types identified, over and above those in [4]. Six of these are major in that they exhibit a single flavour change of  $q_2$  rather than  $q_3$ , which contravenes the expectation that it is the highest total energy quark that will change flavour. This must represent a further variation of the decay process and is discussed below.

The second point to note is that the decay of all Sigma particles considered here are to low energy particle versions, i.e. as stated in [3],  $\Lambda^0$ ,  $\Lambda_c^+$  and  $\Lambda_b^0$  are low confinement energy versions of  $\Sigma^0$ ,  $\Sigma_c^+$  and  $\Sigma_b^0$  respectively. The decays to  $p^+$  and  $n^0$  may also be so categorised as they are low resonance energy versions of  $\Delta^+$  and  $\Delta^0$  respectively. The reason why the Sigma particles considered here decay so is at present unclear.

It is believed that the above feature is related to the third point, the lack of multiple decay paths. All but two of the Sigma particles here exhibit a single decay path, all to Lambda particles. The two with multiple decay paths are first  $\Sigma^+$ , decaying to  $p^+$  and  $n^0$  with roughly equal branching fractions near 50/50, and to  $\Lambda^0$ , but with only a 0.12% branching fraction. Secondly,  $\Sigma^-$  decays to  $n^0$  and  $\Lambda^0$ , predominately the former at 99.85% leaving only 0.15% for the decay to  $\Lambda^0$ . Once again the reasons/mechanisms behind these features is not clear.

The final point of interest is the most important and is the decay process variation represented by Decay Types  $1\phi$ ,  $2\phi$ , 7, 9, and 10. There are two variants,  $1\phi$  and  $2\phi$ , in which  $q_2$  changes flavour to a lower level quark while 7, 9, and 10 involve  $q_2$  changing flavour to a higher level quark.. There is however, a common feature in that Decay Types  $1\phi$  and  $2\phi$  apply to decaying particles that have a quark complement of  $(ddq_3)$ , where  $q_3$  is s, c and b respectively, while Decay Types 7, 9, and 10 apply to decaying particles with a quark complement of  $(uuq_3)$ , where again  $q_3$  is s, c and b respectively. This feature explains the direction of the flavour change of  $q_2$ , but what triggers its change rather than  $q_3$  is again unclear.

With regard to the decay process itself, for the  $1\phi$  and  $2\phi$  Type decays, the process is as described in [3] except for the lower energy quark changing flavour and it is a question of how this is triggered. In the case of 7, 9, and 10,  $q_2$  must gain matter energy before it can change flavour. Such a gain can only come from its own resonance/confinement energy or via an exchange of energy with  $q_3$  as described in [4] Section 3.1. The further Addendums may help to clarify this.

Finally, it should be noted that these are interim conclusions which may be augmented/amended in the forthcoming further Addendums.

### References.

- [1] Wikipedia, *List of Baryons*, en.wikipedia.org.
- [2] Particle Data Group, *Particle Listings*, pdg.lbl.gov.
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